

[25101]

SPECIAL DRIVE - DECEMBER - 2022

M.C.A. DEGREE EXAMINATIONS

SECOND SEMESTER

Paper - I : PROBABILITY, STATISTICS AND QUEUING THEORY

(2016-17 and 2017-18 Admitted Batches)

Time : 3 Hours

Maximum Marks: 75

## SECTION - A

Answer ALL questions.

(4×15=60)

1. a) From vessel containing 3 white and 5 black balls, 4 balls are transferred into an empty vessel. From this vessel a ball is drawn and is found to be white. What is the probability that out of four balls transferred 3 are white and 1 is black.
- b) If X is continuous write random variable with probability density function.

$$f(x) = \begin{cases} \frac{\sin x}{2} & \text{for } 0 \leq x \leq \pi \\ 0 & \text{elsewhere} \end{cases}$$

Find the mean, mode median of the distribution.

(OR)

- c) If A and B are two events and the probability  $P(B) \neq 1$ , Prove that

$$P(A|\bar{B}) = \frac{P(A) - P(A \cap B)}{1 - P(B)} \quad \text{and} \quad \text{hence} \quad \text{deduce} \quad \text{that}$$

$$P(A \cap B) \geq P(A) + P(B) - 1.$$

- d) Let X be a continuous random variable having probability density function.

$$f(x) = \begin{cases} 2e^{-2x} & \text{for } x > 0 \\ 0 & \text{elsewhere} \end{cases}$$

Find Moment Generating Function and obtain  $E(x)$  and  $E(x^2)$  by differentiating the Moment Generating Function.

2. a) Derive mean and variance of binomial distribution.  
 b) Let X be normally distributed with mean  $\mu = 10$  and standard deviation  $\sigma = 2$ . Find  
 i)  $P(9 < X < 13)$  ii)  $P(X < 12)$  iii)  $P(X > 12)$  and  $P(X < 10)$

(OR)

- c) Briefly explain about t-test, F-test and  $\chi^2$ -tests.  
 d) Calculate the coefficient of correlation and the two lines of regression for the following data.

Price (X)	:	14	16	17	18	19	20	21	22	23
Demand (Y)	:	84	78	70	75	66	67	62	58	60

3. a) A die was thrown 9000 times and of these 3220 yielded a 3 or 4. Is this consistent with the hypothesis that the die was unbiased?  
 b) Explain most important desirable properties of good estimate.

(OR)

- c) Let p be the probability that a coin will fall head in a single toss in order to test  $H_0: p = \frac{1}{2}$  against  $H_1: p = \frac{3}{4}$ . The coin is tossed 5 times and  $H_0$  is rejected if more than 3 heads are obtained. Find the probability of type-I error and power of the test.  
 d) Write about formulations of Null hypothesis.

4. a) To compare two kinds of bumper guards, 6 of each kind were mounted on a car and then the car has run into a concrete wall. The following are the costs of repairs:

Guard 1	107	148	123	165	102	119
Guard 2	134	115	112	151	133	129

Use the 0.01 level of significance to test whether the difference between two sample means is significant.

- b) Explain (M/M): (FCFS) queuing model and find the expected line length  $E(L_s)$ .

(OR)

- c) In a given M / M / 1 queue, the arrival rate  $\lambda = 7$  customers/hour and service rate  $h = 10$  customer/hour. Find  $P(X \geq 5)$ , where X is the number of customers in the system.  
 d) Explain Kendall's notation of a queuing system.

## SECTION - B

Answer any FIVE questions.

(5×3=15)

5. a) If  $P(A) = \frac{7}{3}$ ,  $P(B) = \frac{9}{13}$  and  $P(A \cap B) = \frac{4}{13}$ , find  $P\left(\frac{A}{B}\right)$ .
- b) State Bayesian rule for conditional probability.
- c) A continuous random variable X has a. d. f.  $f(x) = 3x^2$ ,  $0 \leq x \leq 1$ . Find 'a' such that  $p(X \leq a) = p(X > a)$
- d) The mean and variance of binomial distribution are 4 and 3 respectively. Find  $p(x \geq 1)$ .
- e) What is Unbiased estimator.
- f) What are the advantages Multiple regression?
- g) Write the characteristics of queuing theory.
- h) Define M/M/2 queueing model.
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